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21EC33

Third Semester B.E. Degree Examination, June/July 2023 Basic Signal Processing

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Define vector space and list out the eight rules that satisfies addition and scalar multiplication. (05 Marks)
- b. For which right hand side vector (b_1, b_2, b_3) have solution to the system. (08 Marks)

$$\begin{bmatrix} 1 & 4 & 2 \\ 2 & 8 & 4 \\ -1 & -4 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}$$
- c. Define column space and null space of the matrix. (07 Marks)

OR

- 2 a. Determine the complete solution $x = x_n + x_p$ to the system (05 Marks)

$$\begin{bmatrix} 1 & 2 & 2 \\ 2 & 4 & 5 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} 1 \\ 4 \end{bmatrix}$$
- b. Find the best straight line fit (least square) to the measurement $b = 4$ at $t = -2$, $b = 3$ at $t = -1$, $b = 1$ at $t = 0$ and $b = 0$ at $t = 2$. Then find the projection of b on to the column space of A (08 Marks)
- c. Apply the Gram – Schmidt process for the independent vectors (07 Marks)

$$a = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}, b = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, c = \begin{bmatrix} 2 \\ 1 \\ 0 \end{bmatrix}$$
 to obtain an orthonormal basis.

Module-2

- 3 a. Find the eigen values and eigen vectors of $A = \begin{bmatrix} 3 & 4 & 2 \\ 0 & 1 & 2 \\ 0 & 0 & 0 \end{bmatrix}$. Check that $\lambda_1 + \lambda_2 + \lambda_3$ equals the trace and $\lambda_1 \lambda_2 \lambda_3$ equals the determinant. (08 Marks)
- b. For the matrix $A = \begin{bmatrix} 1 & -1 \\ 2 & 4 \end{bmatrix}$, solve the differential equation $\frac{du}{dt} = Au, u(0) = \begin{bmatrix} 0 \\ 6 \end{bmatrix}$. What are the two pure exponential solutions? (12 Marks)

OR

- 4 a. If $A = \begin{bmatrix} 4 & 2 & -2 \\ -5 & 3 & 2 \\ -2 & 4 & 1 \end{bmatrix}$ and eigen vector matrix $S = \begin{bmatrix} 2 & 1 & 0 \\ 1 & 1 & 1 \\ 4 & 2 & 1 \end{bmatrix}$. Determine the diagonalization matrix $\Lambda = S^{-1}AS$ (08 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

- b. For the matrix $A = \begin{bmatrix} 1 & 2 \\ 3 & 6 \end{bmatrix}$, find the eigen values, eigen vector v_1, v_2 and $A^T A$. Then find u_1, u_2 and recover A using Singular Value Decomposition (SVD). (12 Marks)

Module-3

- 5 a. Define signals and systems. (04 Marks)
 b. $x(n) = [2, 2, 2, 2, -2, -2, -2, -2]$. Sketch i) $x(n-3)$ ii) $x(2n+3)$. (06 Marks)
 c. Determine whether the system $y(n) = nx(n)$ is
 i) Stable
 ii) Memory
 iii) Causal
 iv) Time invariant
 v) Linear (10 Marks)

OR

- 6 a. Sketch the signal $x(n) = u(n+10) - 2u(n) + u(n-6)$
 $y(n) = 2n[u(n) - u(n-6)]$ (10 Marks)
 b. Sketch the following signals
 i) $x(2n)$
 ii) $x(3n-1)$
 iii) $x(n)u(1-n)$ if $x(n) = [3, 2, 1, 0, 1, 2, 3]$ (10 Marks)

Module-4

- 7 a. Derive an expression for convolution sum for Linear Time Invariant (LTI) system. (04 Marks)
 b. Compute $y(n) = u(n) * u(n)$ using graphical method. (08 Marks)
 c. Compute $y(n) = x(n) * h(n)$, where $x(n) = u(n)$ and $h(n) = \left(\frac{3}{4}\right)^n u(n)$ using graphical method. (08 Marks)

OR

- 8 a. Show that convolution posses the associative and distributive property. (08 Marks)
 b. For the impulse response $h(n) = 2u(n) - 2u(n-5)$. Determine whether the system
 i) Memoryless
 ii) Stable
 iii) Causal (06 Marks)
 c. What is step response? Evaluate the step response of the LTI system whose impulse response in $h(n) = \left(\frac{1}{2}\right)^n u(n)$. (06 Marks)

Module-5

- 9 a. Find the z-transform and mention ROC of the following signals
 i) $x(n) = [1, 2, 3, 4, 0, 7]$
 ii) $x(n) = [1, 2, 3, 4, 0, 7]$
 iii) $x(n) = [1, 2, 3, 4, 0, 7]$ (03 Marks)

- b. Find the z-transform of the signal $x(n) = a^n u(-n-1)$ with ROC diagram. (05 Marks)
- c. Using the properties of the z-transform, find the z-transform of the following signals
- $x(n) = a^n \cos \Omega_0 n u(n)$
 - $x(n) = u(n-2) * \left(\frac{2}{3}\right)^n u(n)$ (12 Marks)

OR

- 10 a. Using partial fraction expansion method find the inverse z-transform of

$$x(z) = \frac{1 - z^{-1} + z^{-2}}{\left(1 - \frac{1}{2}z^{-1}\right)(1 - 2z^{-1})(1 - z^{-1})} \text{ for}$$

- ROC $1 < |z| < 2$
 - ROC $\frac{1}{2} < |z| < 2$
 - ROC $|z| < \frac{1}{2}$ (08 Marks)
- b. A causal system has an input $x(n] = \delta(n) + \frac{1}{4}\delta(n-1) + \frac{1}{8}\delta(n-2)$ and output $y(n) = \delta(n) - \frac{3}{4}\delta(n-1)$. Find the transfer function of the system. (04 Marks)
- c. The LTI system is $H(z) = \frac{3 - 4z^{-1}}{1 - 3.5z^{-1} + 1.5z^{-2}}$. Specify ROC of $H(z)$ and determine $h(n)$ for the following conditions
- The system is stable
 - The system is causal
 - The system is anticausal (08 Marks)
